

CSc 120

Introduction to Computer Programming II

05: Abstract Data Types
Stacks and Queues

Abstract Data Types

Abstract Data Types

An *abstract data type (ADT)* describes a set of data values and associated operations that are specified independent of any particular implementation.

An ADT is a logical description of how we view the data and the operations allowed on that data.

- describes *what* the data represents
- not *how* is the data represented

The data is *encapsulated*.

Abstract Data Types

Because the data is *encapsulated* we can change the underlying implementation without affecting the *logical* way the ADT behaves.

- the logical description remains the same
- the operations remain the same (abstractly)

Example:

- lists
 - Python built-in lists
 - linked lists

Abstract Data Types

Consider the ADT definition of a list.

Lists:

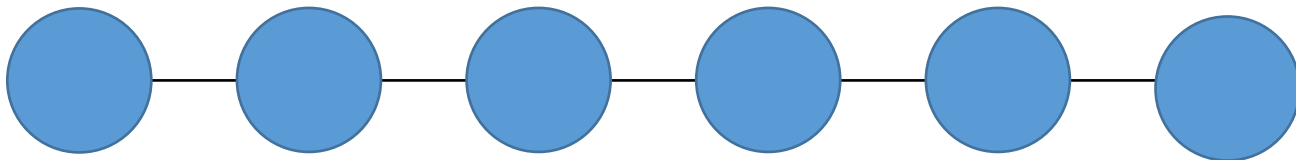
- logical description
 - linear ordering of elements
 - elements can be inserted or deleted from any location
- operations
 - len, indexing, slicing, in, concatenation, insert, delete, ...

linear data structures

Linear data structures

A *linear* data structure is a collection of objects with a straight-line ordering among them

- each object in the collection has a *position*
- for each object in the collection, there is a notion of the object *before* it or *after* it



Data structures we've seen

Linear

- Python lists
- Linked lists

Not linear

- Dictionaries*
- Sets

*Prior to Python v7

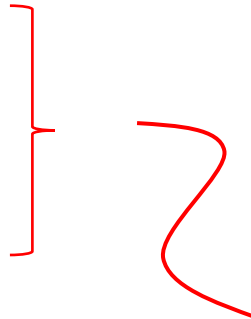
Today's topic

Linear

- Python lists
- Linked lists
- Stacks
- Queues
- Dequeues

Not linear

- Dictionaries*
- Sets



Key property: the way in which objects are added to, and removed from, the collection

*Prior to Python v7

stacks

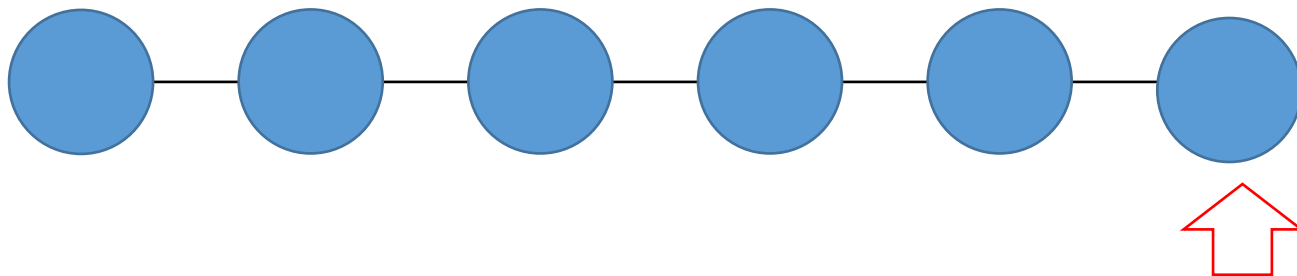
EXERCISE-whiteboard

- Think of a stack of plates in a cafeteria.
- What are some of the logical operations that you would specify for a stack of plates?
- Describe three operations.

The Stack ADT

A *stack* is a linear data structure where objects are inserted or removed only at one end

- all insertions and deletions happen at one particular end of the data structure
- this end is called the *top* of the stack
- the other end is called the *bottom* of the stack



insertions and deletions
happen at one end

Stacks: insertion of values

Insertion of a sequence
of values into a stack:

5 17 33 9 43

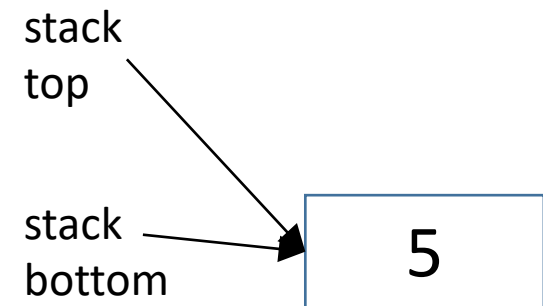
stack
top None

stack
bottom None

Stacks: insertion of values

Insertion of a sequence
of values into a stack:

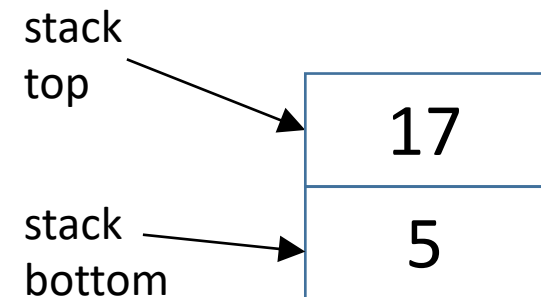
5 17 33 9 43



Stacks: insertion of values

Insertion of a sequence
of values into a stack:

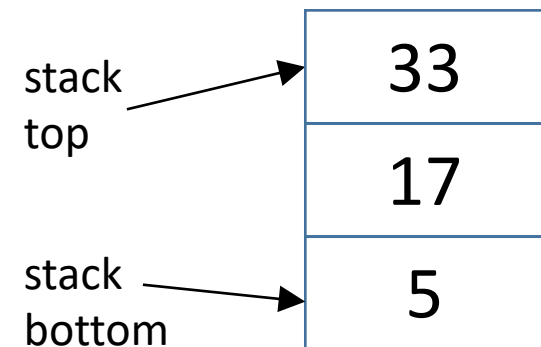
5 17 33 9 43



Stacks: insertion of values

Insertion of a sequence
of values into a stack:

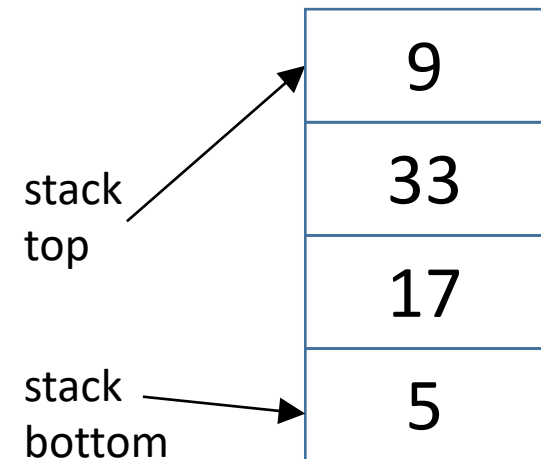
5 17 33 9 43



Stacks: insertion of values

Insertion of a sequence
of values into a stack:

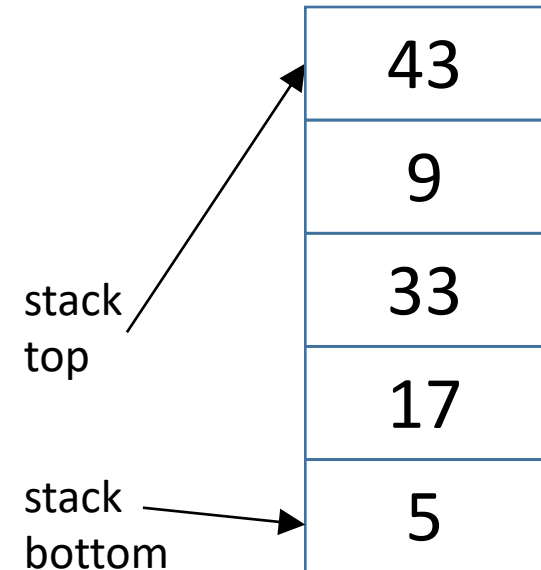
5 17 33 **9** 43



Stacks: insertion of values

Insertion of a sequence
of values into a stack:

5 17 33 9 **43**

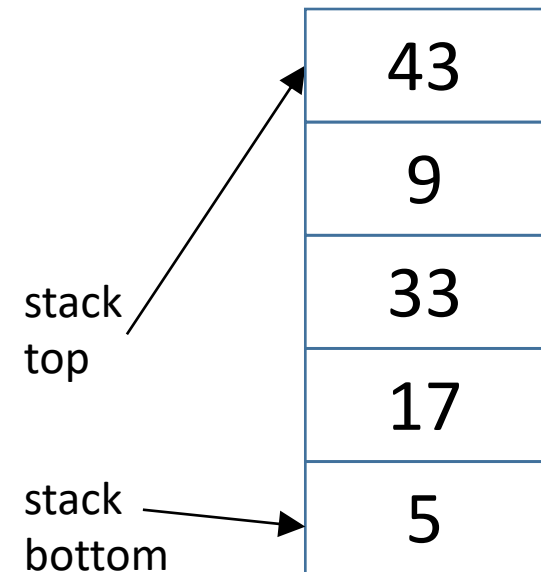


Stacks: insertion of values

5 17 33 9 43



order in which values were inserted



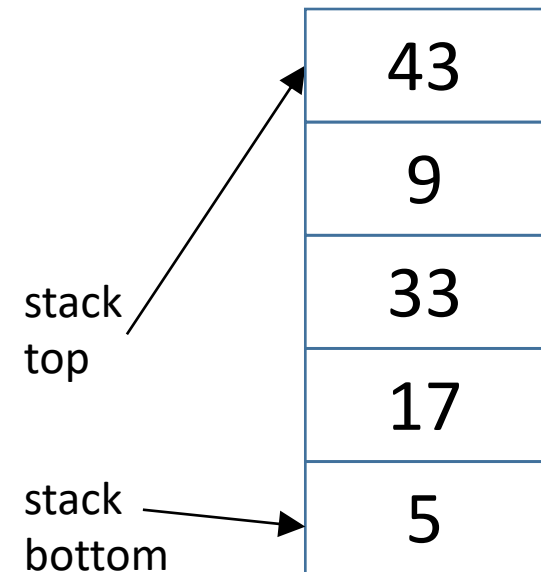
Stacks: removal of values

5 17 33 9 43



order in which values were inserted

Removing values from
the stack:



Stacks: removal of values

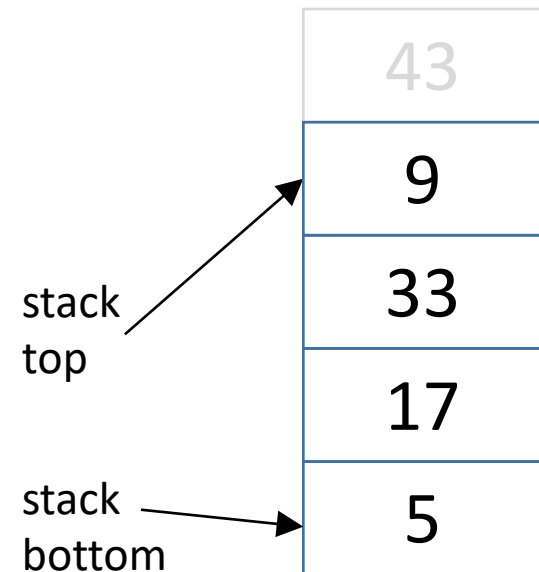
5 17 33 9 43



order in which values were inserted

Removing values from
the stack:

43



Stacks: removal of values

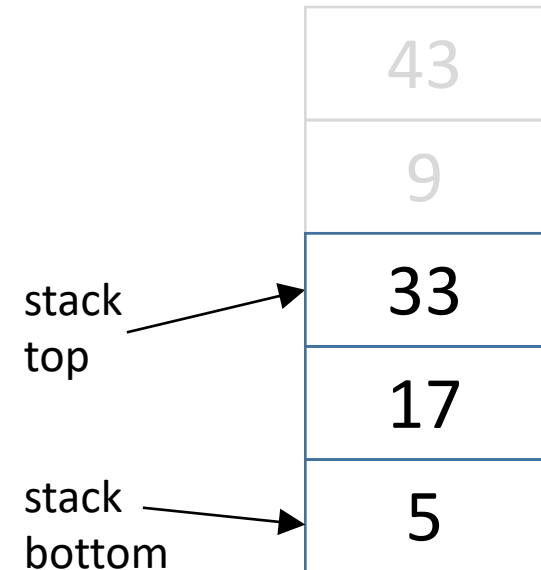
5 17 33 9 43



order in which values were inserted

Removing values from
the stack:

43 9



Stacks: removal of values

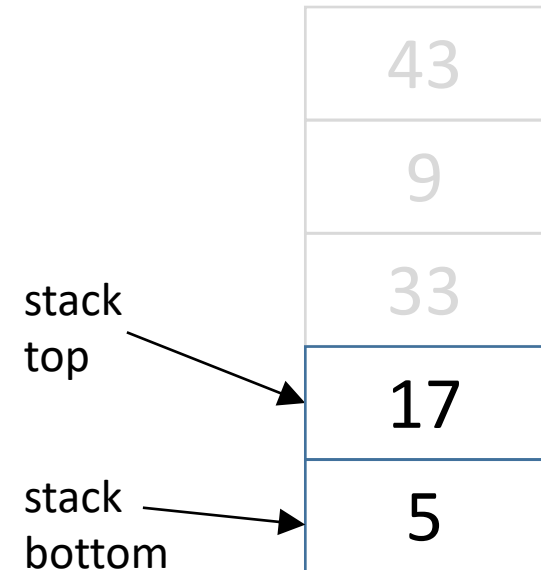
5 17 33 9 43



order in which values were inserted

Removing values from
the stack:

43 9 33



Stacks: removal of values

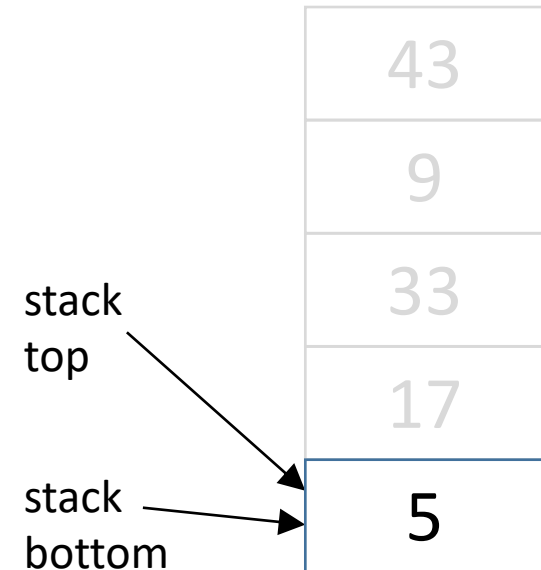
5 17 33 9 43



order in which values were inserted

Removing values from
the stack:

43 9 33 17



Stacks: removal of values

5 17 33 9 43



order in which values were inserted

Removing values from
the stack:

43 9 33 17 5

stack
top

None

stack
bottom

None



Stacks: removal of values

5 17 33 9 43



order in which values were inserted

Removing values from
the stack:

43 9 33 17 5



order in which values were removed

Stacks: LIFO property

5 17 33 9 43



order in which values were inserted

Removing values from
the stack:

43 9 33 17 5



order in which values were removed

values are removed in
reverse order from the
order of insertion

"LIFO order"
Last in, First out

The Stack ADT

A *stack* is a linear data structure where objects are inserted or removed only at one end

- all insertions and deletions happen at one particular end of the data structure
- this end is called the *top* of the stack
- the other end is called the bottom of the stack

Operations

- insert at the top (called push)
- delete from the top (called pop)

Methods for a Stack class

- `Stack()` : creates a new empty stack
- `push(item)` : adds *item* to the top of the stack
 - returns nothing
 - modifies the stack
- `pop()` : removes the top item from the stack
 - returns the removed item
 - modifies the stack
- `is_empty()` : checks whether the stack is empty
 - returns a Boolean

EXERCISE

```
>>> s = Stack()
```

```
>>> s.push(4)
```

```
>>> s.push(17)
```

```
>>> s.push(5)
```

```
>>> x = s.pop()
```

```
>>> y = s.pop()
```

← *what does the stack `s` look like here?
what are the values of `x` and `y`?*

EXERCISE

```
>>> s = Stack()
```

```
>>> s.push(4)
```

```
>>> s.push(17)
```

```
>>> s.push(5)
```

```
>>> x = s.pop()
```

```
>>> y = s.pop()
```

```
>>> s.push(x)
```

```
>>> s.push(y)
```

← *what does the stack s look like here?*

EXERCISE-ICA-16, prob 2

Implement the Stack class below. Use a Python list to hold the data.

Note: given a list alist, the Python method alist.pop() removes the last element of the list.

class Stack:

create a Stack

def __init__(self):

self._items = ?

adds item to the "top"

def push(self, item):

?

removes the last item from the Stack

def pop(self):

?

Implementing a Stack class

```
class Stack:
```

```
    # the top of the stack is the last item in the list
```

```
    def __init__(self):
```

```
        self._items = []
```

```
    def push(self, item):
```

```
        self._items.append(item)
```

```
    def pop(self):
```

```
        return self._items.pop()
```

*removes and returns
the last item in a list*



EXERCISE- Whiteboard

```
>>> s1 = Stack()
```

```
>>> s1.push(4)
```

```
>>> s1.push(17)
```

```
>>> s2 = Stack()
```

```
>>> s2.push(s1.pop())
```

```
>>> s2.push(s1.pop())
```

```
>>> s1.push(s2.pop())
```

```
>>> s1.push(s2.pop())
```

← *what does the stack s1 look like here?*

stacks: applications

An application: balancing parens

IDLE (the Python shell) matches up left and right parens (), brackets [], and braces { }

```
>>> x = [1, 2, [3, 4, [5], 7], 8]
```

How does it figure out how far back to highlight?

An application: balancing parens

Basic idea: Match each] with corresponding [

- similarly for (...) and { ... } pairs

- Idea:

- maintain a stack
- on seeing '[' : push the symbol
- on seeing ']' : pop the matching symbol

Example: [1, 2, [3, [4], 5 , [7]]]

Stack (empty)

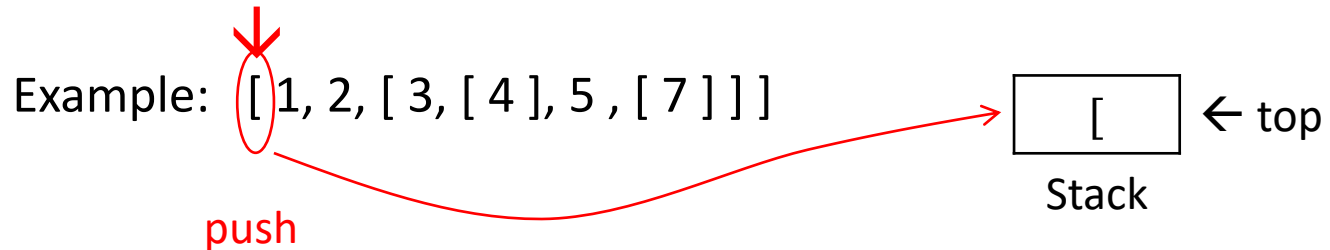
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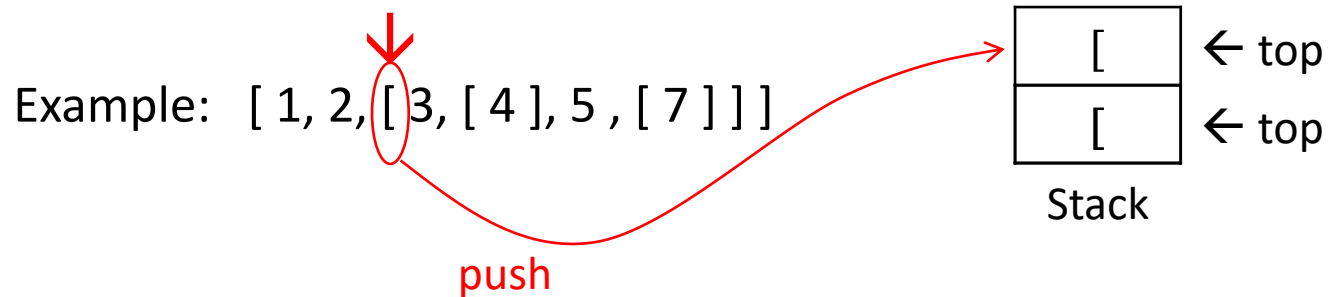
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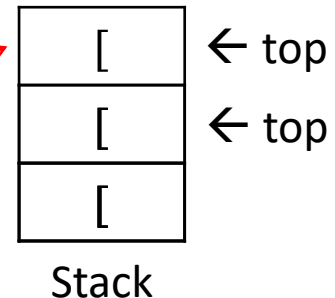
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Example: [1, 2, [3, [4], 5 , [7]]]



push



An application: balancing parens

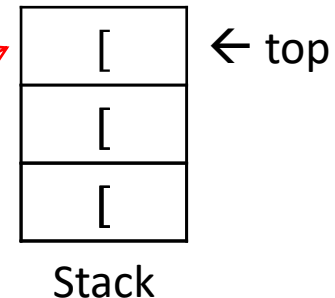
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Example: [1, 2, [3, [4], 5 , [7]]]



matches:
pop

An application: balancing parens

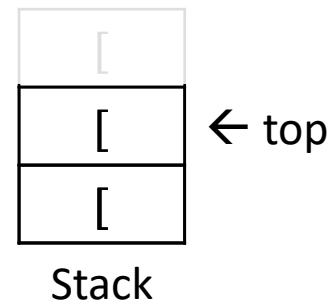
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An application: balancing parens

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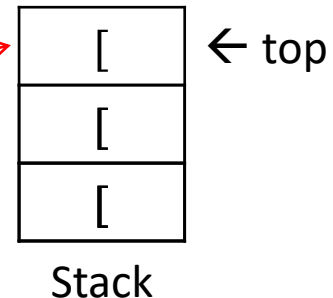
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Example: [1, 2, [3, [4], 5 , [7]]]



push



An application: balancing parens

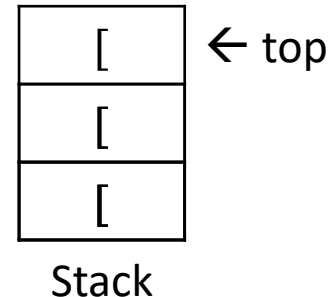
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An application: balancing parens

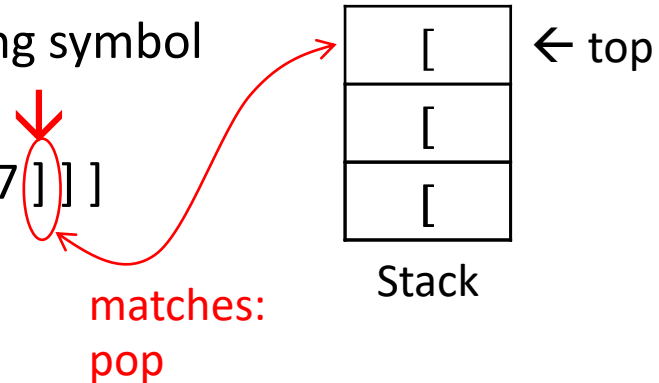
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Example: [1, 2, [3, [4], 5 , [7]]]



An application: balancing parens

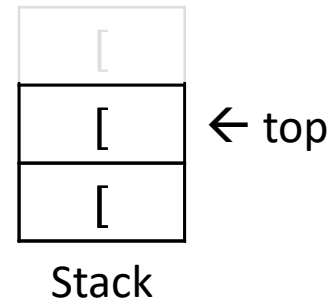
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An application: balancing parens

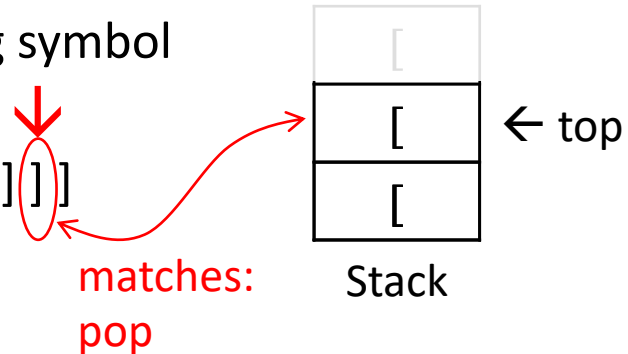
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An application: balancing parens

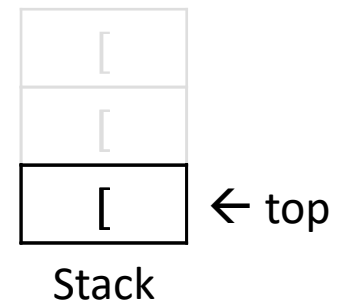
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An application: balancing parens

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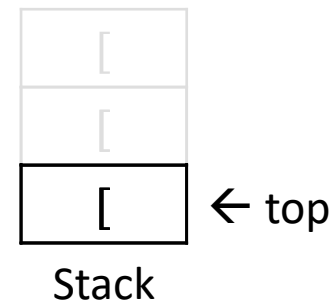
— Idea:

- maintain a stack
- on seeing '[' : push the symbol
- on seeing ']' : pop the matching symbol

Example: [1, 2, [3, [4], 5 , [7]]]



matches:
pop



An application: balancing parens

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- maintain a stack
- on seeing '[' : push the symbol
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Example: [1, 2, [3, [4], 5 , [7]]]

Stack (empty)

Note: the stack should be empty when the input has been processed

An application: balancing parens

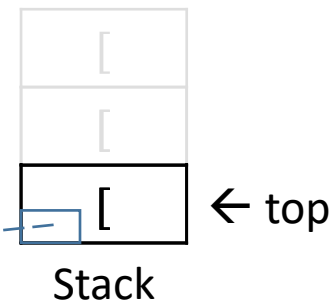
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Example: [1, 2, [3, [4], 5 , [7]]]



Elaboration: Have each stack element keep track of the position of its [

EXERCISE-ICA-17-p.1

Given the Stack class, write a function `reverse(s)` that reverses a string using a stack.

```
class Stack:
    def __init__(self):
        self._items = []

    def push(self, item):
        self._items.append(item)

    def pop(self):
        return self._items.pop()

    def is_empty():
        return self._items == []
```

EXERCISE-ICA-17 p.2

Given the Stack class, write a function `balanced(s)` that returns `True` if the string `s` is balanced with respect to '[' and ']' and `False` otherwise.

```
class Stack:
    def __init__(self):
        self._items = []

    def push(self, item):
        self._items.append(item)

    def pop(self):
        return self._items.pop()

    def is_empty(self):
        return self._items == []
```

EXERCISE-ICA-17 p.3

Change the implementations of the push() and pop() methods so that the top of the stack is at the beginning of the list.

```
class Stack:
    def __init__(self):
        self._items = []

    def push(self, item):
        self._items.append(item)

    def pop(self):
        return self._items.pop()

    def is_empty(self):
        return self._items == []
```

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Web page

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CSc 120: Phylogenetic Trees

This problem brings together many different programming and trees. It is one of the most technically challenging problems in the course.

Background

An [evolutionary tree](#) (also called a [phylogenetic tree](#)) is a diagram showing the evolutionary relationships between organisms. This program involves writing code to construct phylogenetic trees. For example, since programs are sequences of characters, we can use them to construct phylogenetic trees.

Expected Behavior

Write a Python program, in a file `phylo.py`, that behaves as follows:

1. *Read in the input parameters:*
 - Read in the name of an input file using `input()`
 - Read in an integer value `N` using `input('n-gr')`
2. *Read in the input file.* The file format is specified in the file `phylo.txt`.

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Display considerations

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2. *Read in the input file.* The file format is specified on the next slide.

main header: large font, bold

secondary header: medium font, bold

bold font

italics font

Question: how does the web browser figure out how much a given display format should include?

E.g., which text is in boldface, how much is in italics, etc.

Related: Displaying web pages

Web page

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DEPARTMENT OF COMPUTER SCIENCE

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Background

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This program involves writing code to construct phylogenetic trees from the genome sequences of a set of organisms. (Of course, there is an inherent difficulty about the techniques we use and the code we write, since programs are sequences of characters, we could just apply this approach to sets of programs.)

Expected Behavior

Write a Python program, in a file **phylo.py**, that behaves as specified below.

1. *Read in the input parameters:*
 - Read in the name of an input file using **input**
 - Read in an integer value N using **input('n-gr')**
2. *Read in the input file.* The file format is specified in the

HTML source

```
</head>
<body bgcolor="white">
<p>


<h1>CSc 120: Phylogenetic Trees</h1>

This problem brings together many different programming construc
techniques we covered over the course of the semester including:
manipulation, (Python) lists, dictionaries, tuples, classes,
list comprehensions, and trees. It is one of the most
technically challenging programs assigned in this class this sem
think it's also one of the most interesting.

<h2>Background</h2>
An <a href="http://evolution.berkeley.edu/evolibrary/article/phy
evolutionary tree</a> (also called a
<a href="https://en.wikipedia.org/wiki/Phylogenetic_tree"
target="_blank">phylogenetic tree</a>) is a tree that express
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<p/>
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apply this approach to sets of programs.)

<h2>Expected Behavior</h2>
Write a Python program, in a file <b><tt>phylo.py</tt></b>, that
behaves as specified below.
<p/>
<ol>
<li>
<i>Read in the input parameters</i>:

```

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Web page

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Expected Behavior

Write a Python program, in a file **phylo.py**, that behaves as specified below.

1. **Read in the input parameters:**
 - Read in the name of an input file using **input()**.
 - Read in an integer value **N** using **input('n-gr')**.
2. **Read in the input file.** The file format is specified in the file **phylo.py**.

HTML source

```
</head>
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manipulation, (Python) lists, dictionaries, tuples, classes,
list comprehensions, and trees. It is one of the most
technically challenging programs assigned in this class this sem
think it's also one of the most interesting.

<h2>Background</h2>
An <a href="http://evolution.berkeley.edu/evolibrary/article/phy
evolutionary tree"> (also called a
<a href="https://en.wikipedia.org/wiki/Phylogenetic_tree"
target="_blank">phylogenetic tree</a>) is a tree that express
evolutionary relationships between a set of organisms.
<p/>
This program involves writing code to construct phylogenetic tre
the genome sequences of a set of organisms. (Of course, there i
inherently genetic about the techniques we use and the code we w
example, since programs are sequences of characters, we could ju
apply this approach to sets of programs.)

<h2>Expected Behavior</h2>
Write a Python program, in a file <b><tt>phylo.py</tt></b>, that
behaves as specified below.
<p/>
<ol>
<li>
<i>Read in the input parameters</i>:

```

Related: Displaying web pages

HTML source

"tags"

`<h1>` : "open header 1"

`</h1>` : "close header 1"

`<h2>` : "open header 2"

`</h2>` : "close header 2"

`<i>` : "open italics"

`</i>` : "close italics"

...

```
</head>
<body bgcolor="white">
<p>

<h1>CSc 120: Phylogenetic Trees</h1>
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<h2>Expected Behavior</h2>
Write a Python program, in a file <b><tt>pylo.py</tt></b>, that
behaves as specified below.
<p/>
<ol>
<li>
<i>Read in the input parameters</i>:
```

Related: Displaying web pages

Web page

HTML source

THE UNIVERSITY OF ARIZONA
DEPARTMENT OF COMPUTER SCIENCE

CSc 120: Phylogenetic Trees

This problem brings together many different programming constructs and trees. It is one of the most challenging problems in this class this semester.

Background

An [evolutionary tree](#) (also called a phylogenetic tree) is a tree that expresses the evolutionary relationships between organisms. Constructing phylogenetic trees is a central problem in biology. The genome sequences of a set of organisms. (Of course, there is an inherent genetic about the techniques we use and the code we write. For example, since programs are sequences of characters, we could just apply this approach to sets of programs.)

Expected Behavior

Write a Python program, in a file **phylo.py**, that behaves as specified below.

1. Read in the input parameters:
 - Read in the name of an input file using **input**
 - Read in an integer value N using **input('n-gr')**
2. Read in the input file. The file format is specified in the next section.

```
</head>
<body bgcolor="white">
<p>

<h1>CSc 120: Phylogenetic Trees</h1>
This problem brings together many different programming constructs
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<ol>
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```

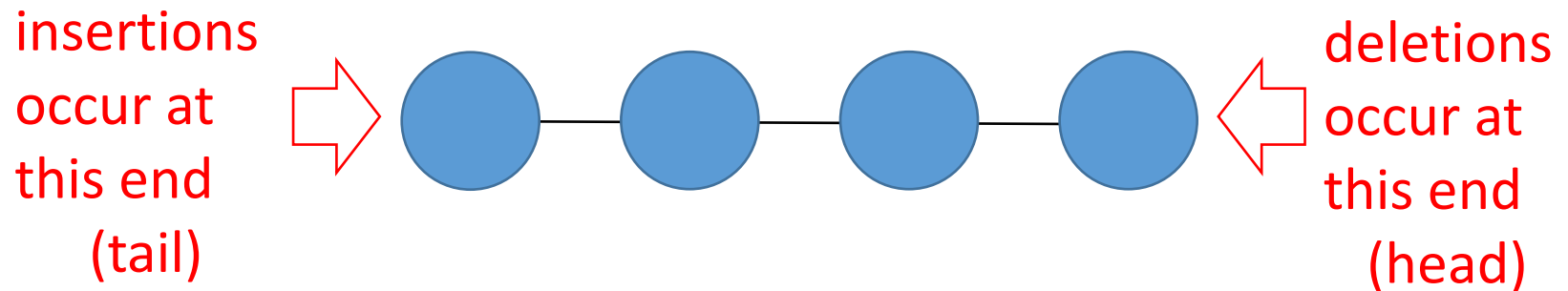
Figuring out how to display different parts of the web page requires matching up “open-” and “close-” HTML tags. This is essentially the same problem as balancing parens.

queues

A Queue ADT

A *queue* is a linear data structure where insertions and deletions happen at different ends

- insertions happen at one end (the queue's "back", or "tail")
- deletions happen at the other end (the queue's "front", or "head")



Queues: insertion of values

Insertion of a sequence
of values into a queue:

5 17 33 9 43

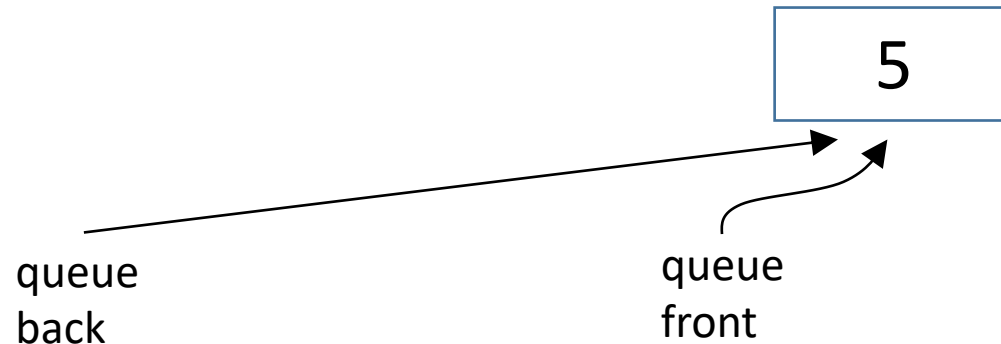
queue
back **None**

queue
front **None**

Queues: insertion of values

Insertion of a sequence
of values into a queue:

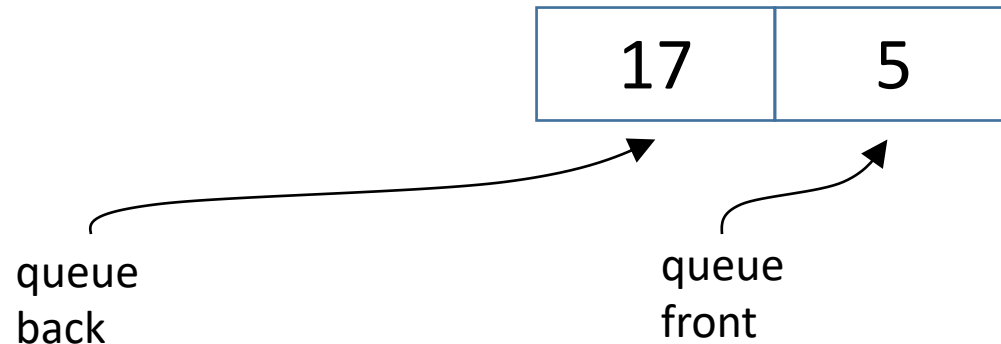
5 17 33 9 43



Queues: insertion of values

Insertion of a sequence
of values into a queue:

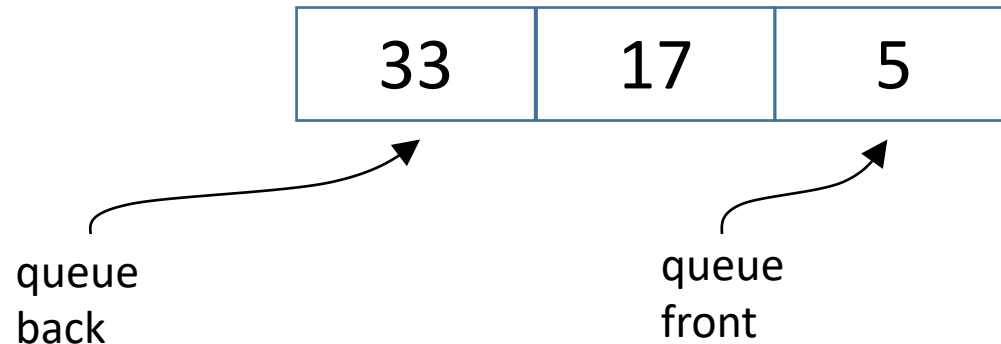
5 17 33 9 43



Queues: insertion of values

Insertion of a sequence
of values into a queue:

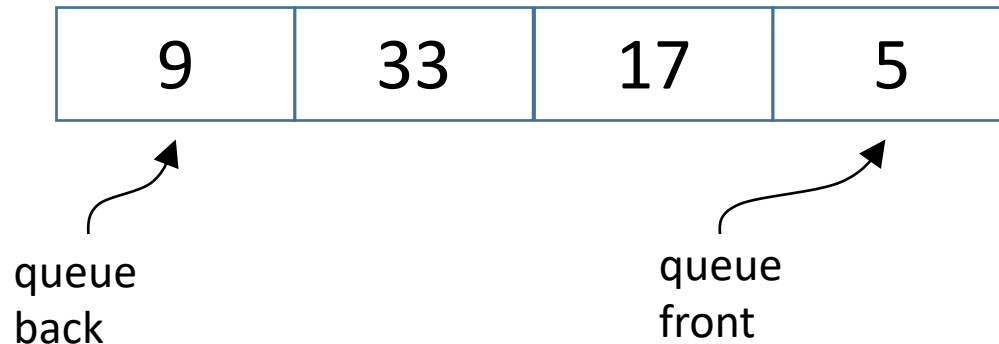
5 17 33 9 43



Queues: insertion of values

Insertion of a sequence
of values into a queue:

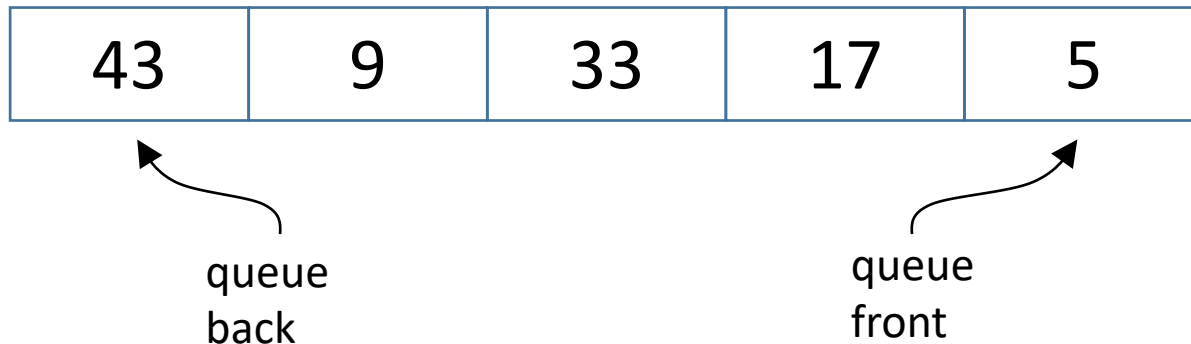
5 17 33 **9** 43



Queues: insertion of values

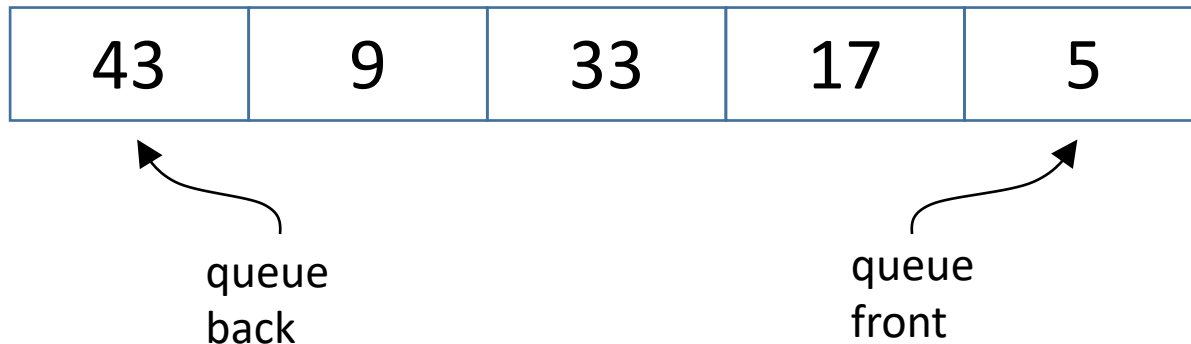
Insertion of a sequence
of values into a queue:

5 17 33 9 **43**



Queues: insertion of values

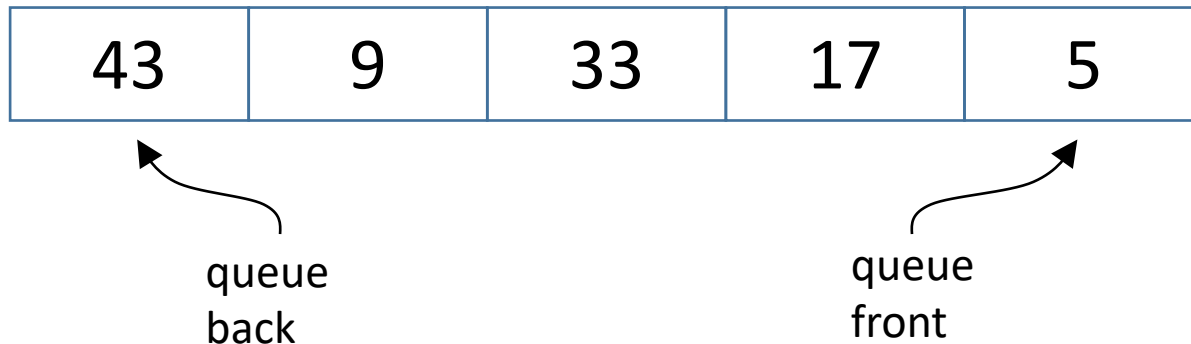
order of insertion —————> 5 17 33 9 43



Queues: removal of values

order of insertion → 5 17 33 9 43

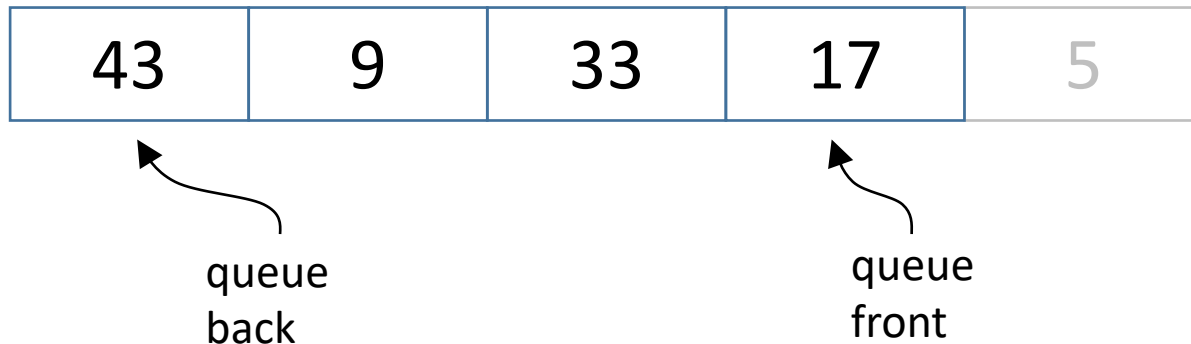
Removing values
from this queue:



Queues: removal of values

order of insertion → 5 17 33 9 43

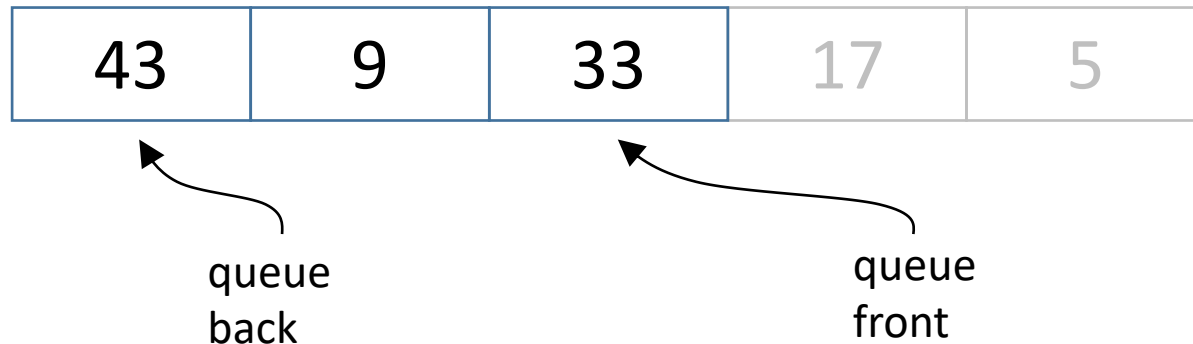
Removing values
from this queue: 5



Queues: removal of values

order of insertion → 5 17 33 9 43

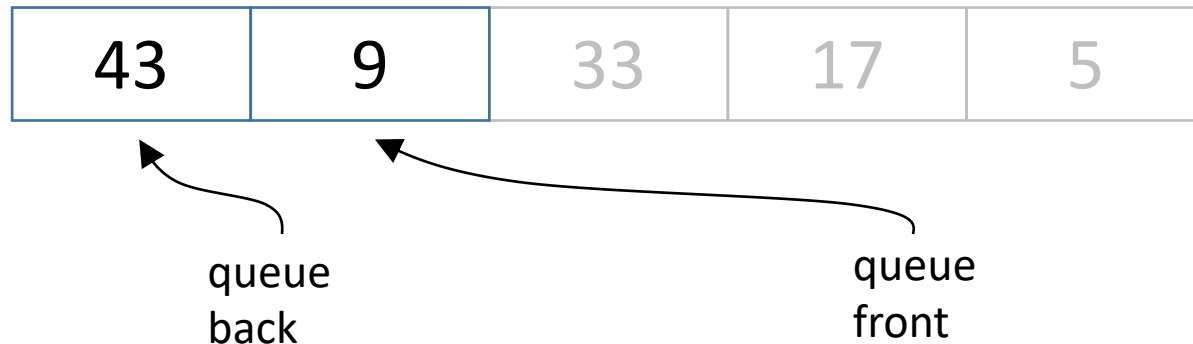
Removing values
from this queue: 5 17



Queues: removal of values

order of insertion → 5 17 33 9 43

Removing values
from this queue: 5 17 33

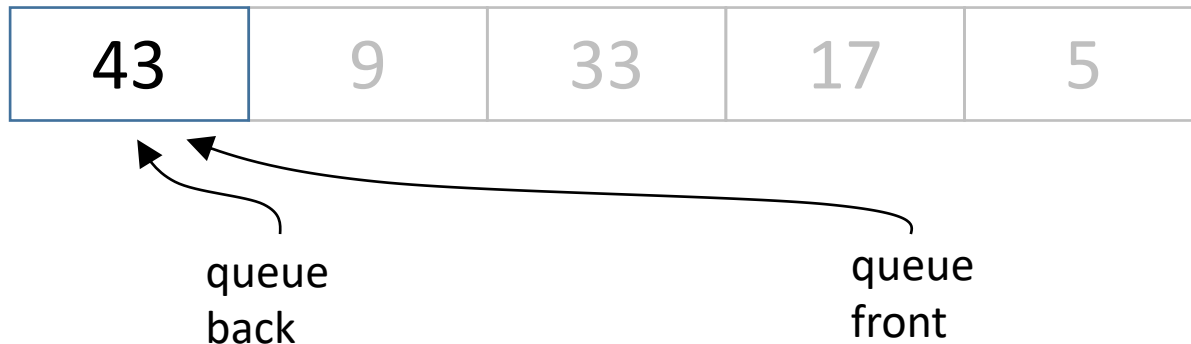


Queues: removal of values

order of insertion → 5 17 33 9 43

Removing values
from this queue:

5 17 33 9



Queues: removal of values

order of insertion —————> 5 17 33 9 43

Removing values
from this queue:

5 17 33 9 43



queue
back **None**

queue
front **None**

Queues: removal of values

order of insertion →

5 17 33 9 43

5 17 33 9 43

order of removal →

Queues: FIFO property

order of insertion →

5 17 33 9 43

5 17 33 9 43

order of removal →

values are removed in
order in which they are
inserted

"FIFO order"
First in, First out

Methods for a queue class

- Queue(): creates a new empty queue
- enqueue(*item*): adds *item* to the back of the queue
 - modifies the queue
 - returns nothing
- dequeue(): removes and returns the item at the front of the queue
 - returns the removed item
 - modifies the queue
- is_empty(): checks whether the queue is empty
 - returns a Boolean
- size(): returns the size of the queue
 - returns an integer

EXERCISE

```
>>> q = Queue()
```

```
>>> q.enqueue(4)
```

```
>>> q.enqueue(17)
```

```
>>> x = q.dequeue()
```

```
>>> q.enqueue(5)
```

```
>>> y = q.dequeue()
```

← *what are the values of x and y?*

EXERCISE

```
>>> q = Queue()
```

```
>>> q.enqueue(4)
```

```
>>> q.enqueue(17)
```

```
>>> x = q.dequeue()
```

```
>>> y = q.dequeue()
```

```
>>> q.enqueue(y)
```

```
>>> q.enqueue(x)
```

```
>>> q.enqueue(y)
```

← *what does the queue q look like here?*

Implementing a queue class

- Use a built-in list for the internal representation
 - Python lists can be added to from the front or the end
- First implementation
 - the head is the n th element
 - the tail is the 0^{th} element
- Second implementation:
 - the head is the 0^{th} element
 - the tail is the n th element

EXERCISE-ICA18-prob 1

Implement a queue with a Python list. Make the front of the queue the nth (last) item in the list.

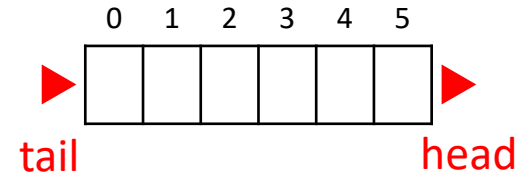
Note: `alist.insert(0,item)` inserts at the front of `alist`

```
class Queue:
```

```
    def __init__(self):
```

```
        def enqueue(self, item):
```

```
        def dequeue(self):
```



Answer: implementation I

```
class Queue:
```

the front of the queue is the last item in the list

```
def __init__(self):
```

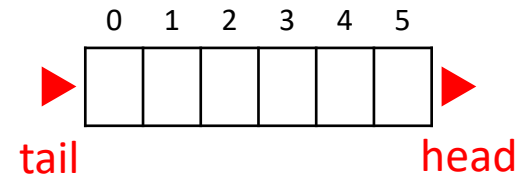
```
    self._items = []
```

```
def enqueue(self, item):
```

```
    self._items.insert(0, item)
```

```
def dequeue(self):
```

```
    return self._items.pop()
```



*removes and
returns the last
item in the list*

Answer: implementation II

```
class Queue:
```

the front of the queue is the first item in the list

```
def __init__(self):
```

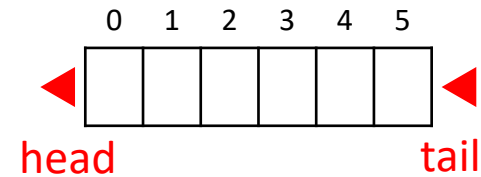
```
    self._items = []
```

```
def enqueue(self, item):
```

```
    self._items.append(item)
```

```
def dequeue(self):
```

```
    return self._items.pop(0)
```



*removes and
returns item 0
from the list*

queues: applications

Application 1: Simulation

- Typical applications simulate problems that require data to be managed in a FIFO manner
 - Hot potato
 - Kids stand in a circle and pass a “hot potato” around until told to stop. The person holding the potato is taken out of the circle. The process is repeated until only one person remains.
- Use a *simulation* to determine which person remains after num "passes" or rounds
 - Person at front of queue "holds" the potato
 - To pass the potato: simulate by dequeue/enqueue
 - After a given number of passes, the person at the front is removed: simulate by dequeue
 - Let's see this in action

EXERCISE-ICA18-prob 2

Write a function `hot_potato(q, num)` that takes a queue `q` and the number of rounds of simulation `num` and eliminates the correct element after `num` rounds.

What operations take an element from the front of the queue and place it at the back of the queue?

Solution

```
def hot_potato(q, num):
```

```
    for i in range(num):
```

```
        x = q.dequeue()
```

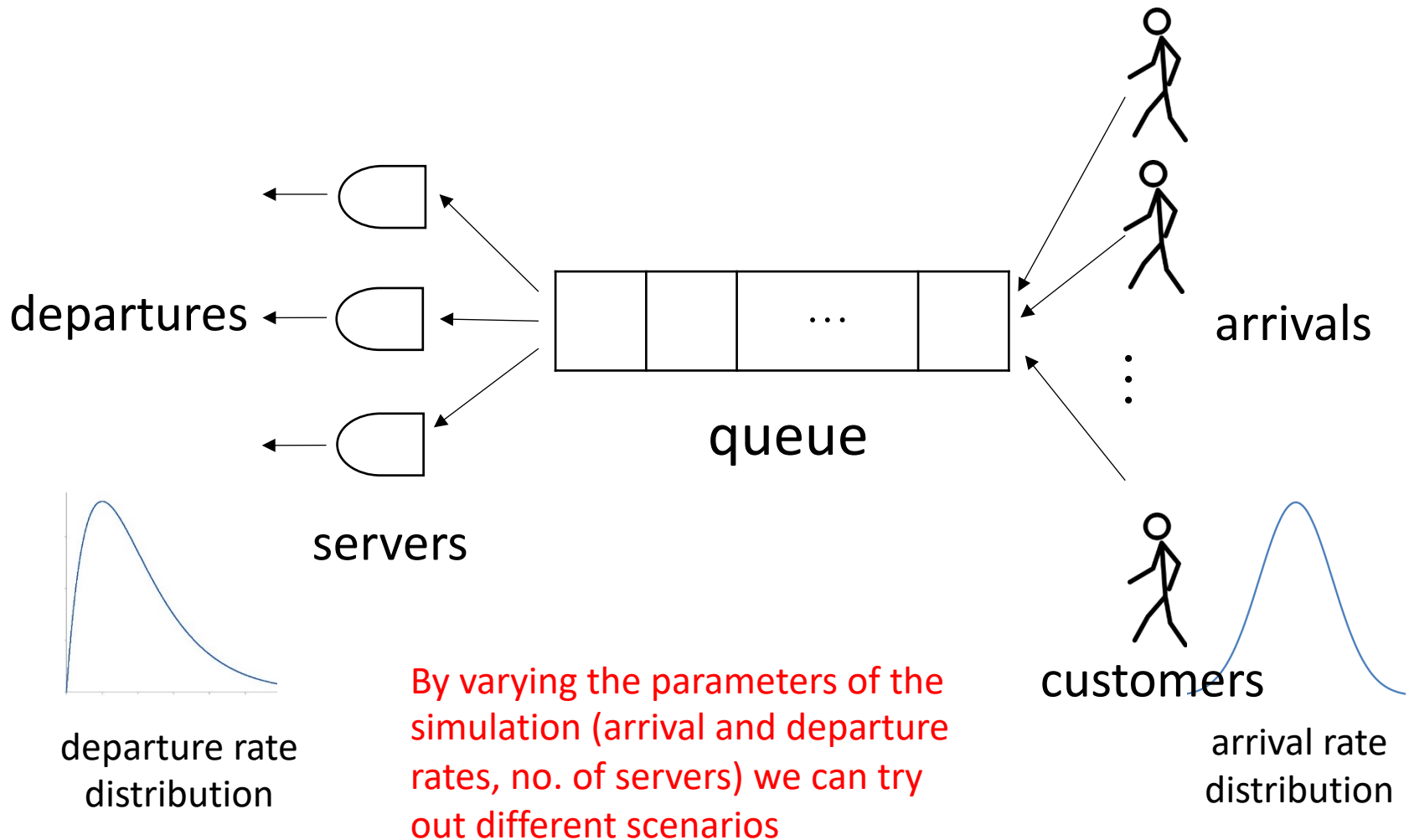
```
        q.enqueue(x)
```

```
    return q.dequeue()
```

Application 2 : Simulation

- Suppose we are opening a grocery store. How many checkout lines should we put in?
 - too few \Rightarrow long wait times, unhappy customers
 - too many \Rightarrow wasted money, space
- Use *simulations* of the checkout process to guide the decision
 - study existing stores to figure out typical shopping and checkout times
 - estimate no. of customers expected at the new location
 - run simulations to determine customer wait time and checkout line utilization under different scenarios

Discrete event simulation



Summary

- Stacks and queues are abstract data types (ADTs)
 - similar in that they are both *linear* data structures
 - items can be thought of as arranged in a line
 - each item has a position and a before/after relationship with the other items
- They differ in the way items are added and removed
 - stacks: items added and removed at one end
 - results in LIFO behavior
 - queues: items added at one end, removed at the other
 - results in FIFO behavior
- They find a wide range of applications in computer science